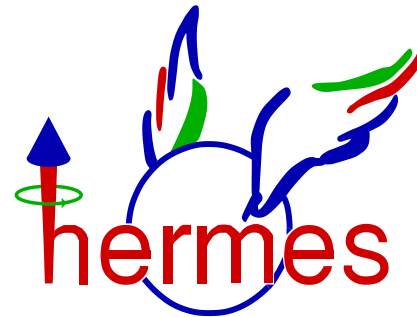

DVCS at HERMES

Orbital Angular Momentum of Partons in Hadrons, Trento, Italy, 2009

Ami Rostomyan

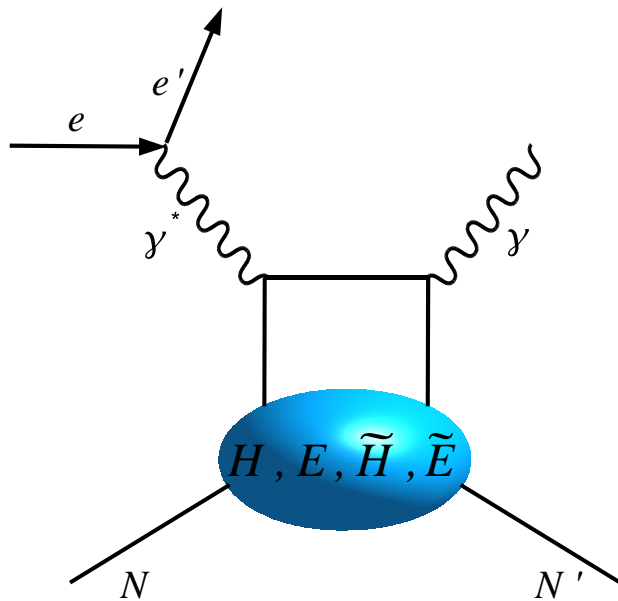
(on behalf of the HERMES collaboration)



probing the orbital angular momentum

- Generalised Parton Distributions (GPDs)

- hard exclusive reactions
 - Deeply Virtual Compton Scattering (DVCS)



$(\gamma^* \rightarrow \gamma): H, E, \tilde{H}, \tilde{E}$ (twist-2, chiral even)

- H and \tilde{H} conserve the nucleon helicity

- E and \tilde{E} describe the nucleon helicity flip

- Ji relation

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H_q(x, \xi, t) + E_q(x, \xi, t)]$$

$$= \frac{1}{2} \Delta \Sigma_q + L_q$$

why DVCS?

- the cleanest probe of GPDs

- theoretical accuracy at NNLO

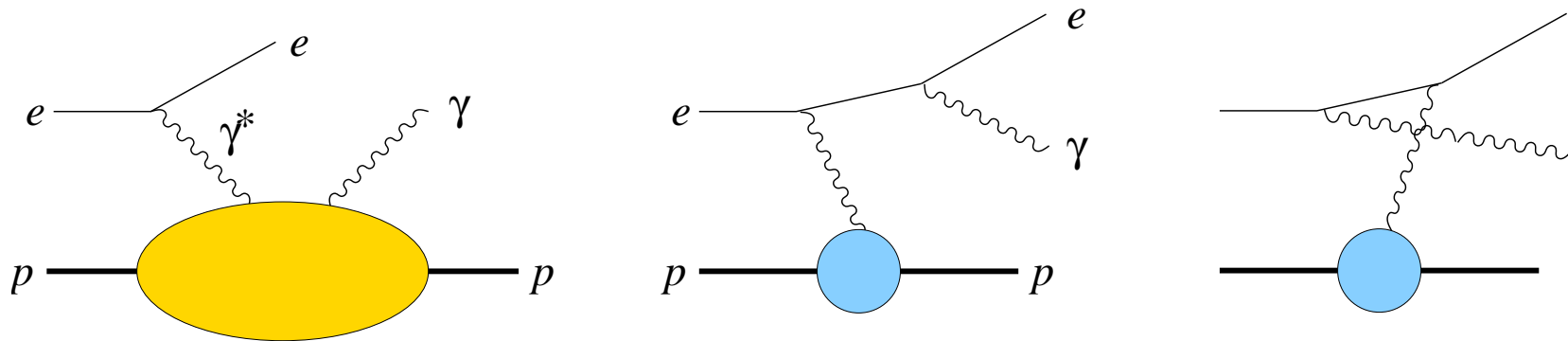
- no gluons in the LO

Compton form factors

- convolutions of GPDs ($F : H, E, \tilde{H}, \tilde{E}$) and hard scattering functions

$$\mathcal{F}(\xi, t) = \sum_q \int_{-1}^1 dx C_q(\xi, x) F^q(x, \xi, t)$$

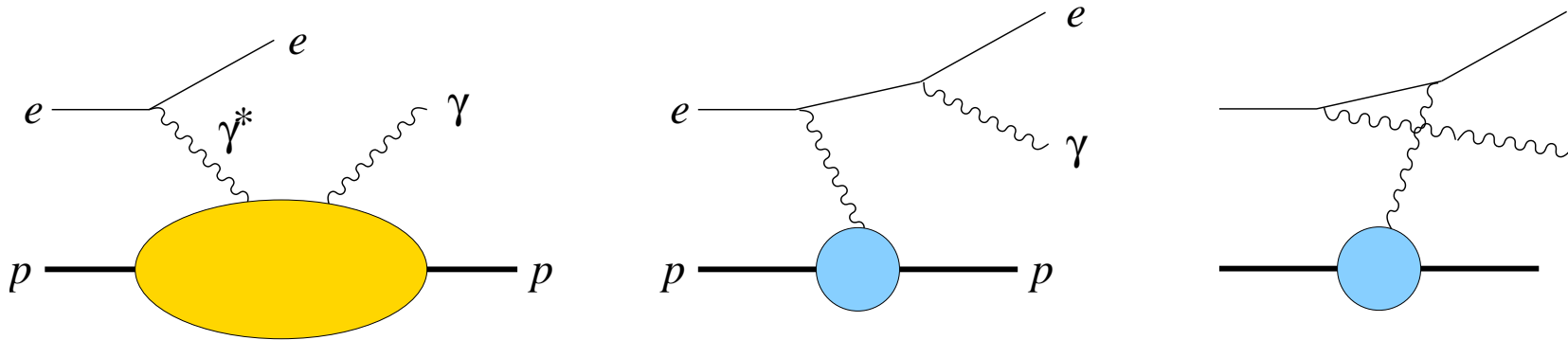
Deeply Virtual Compton Scattering (DVCS)



same initial and final states in DVCS and Bethe-Heitler \Rightarrow Interference!

$$\sigma_{ep} \propto |T_{BH}|^2 + |T_{DVCS}|^2 + \underbrace{T_{BH}T_{DVCS}^* + T_{BH}^*T_{DVCS}}_{\mathcal{I}}$$

Deeply Virtual Compton Scattering (DVCS)



same initial and final states in DVCS and Bethe-Heitler \Rightarrow Interference!

σ_{XY}

$$\sigma_{ep} \propto |T_{BH}|^2 + |T_{DVCS}|^2 + \underbrace{T_{BH}T_{DVCS}^* + T_{BH}^*T_{DVCS}}_{\mathcal{I}}$$

beam:
 P_l

target:
 $S_L S_T$

$$\begin{aligned} d\sigma \sim & d\sigma_{UU}^{BH} + e_l d\sigma_{UU}^I + d\sigma_{UU}^{DVCS} \\ & + e_l P_l d\sigma_{LU}^I + P_l d\sigma_{LU}^{DVCS} \\ & + e_l S_L d\sigma_{UL}^I + S_L d\sigma_{UL}^{DVCS} \\ & + e_l S_T d\sigma_{UT}^I + S_T d\sigma_{UT}^{DVCS} \\ & + P_l S_L d\sigma_{LL}^{BH} + e_l P_l S_L d\sigma_{LL}^I + P_l S_L d\sigma_{LL}^{DVCS} \\ & + P_l S_T d\sigma_{LT}^{BH} + e_l P_l S_T d\sigma_{LT}^I + P_l S_T d\sigma_{LT}^{DVCS} \end{aligned}$$

single spin terms: LU, UL, UT



no pure Bethe-Heitler contribution



project imaginary parts of Compton form factors

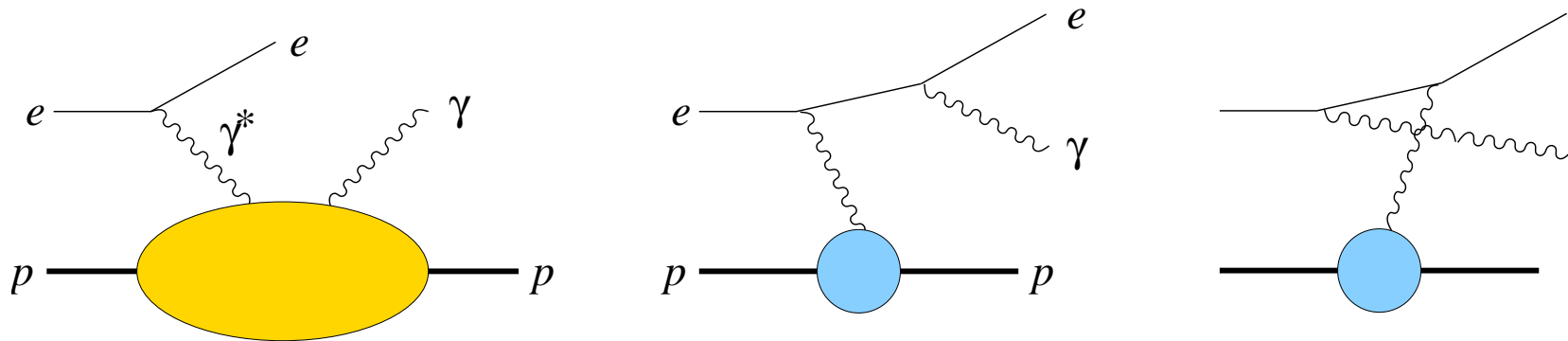
unpolarized and double-spin terms:

UU, LL, LT



project real parts of Compton form factors

Deeply Virtual Compton Scattering (DVCS)



same initial and final states in DVCS and Bethe-Heitler \Rightarrow Interference!

σ_{XY}

$$\sigma_{ep} \propto |\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2 + \underbrace{\mathcal{T}_{BH}\mathcal{T}_{DVCS}^* + \mathcal{T}_{BH}^*\mathcal{T}_{DVCS}}_{\mathcal{I}}$$

beam:
 P_L

target:
 $S_L S_T$

$$\begin{aligned} d\sigma \sim & d\sigma_{UU}^{BH} + e_l d\sigma_{UU}^I + d\sigma_{UU}^{DVCS} \\ & + e_l P_l d\sigma_{LU}^I + P_l d\sigma_{LU}^{DVCS} \\ & + e_l S_L d\sigma_{UL}^I + S_L d\sigma_{UL}^{DVCS} \\ & + e_l S_T d\sigma_{UT}^I + S_T d\sigma_{UT}^{DVCS} \\ & + P_l S_L d\sigma_{LL}^{BH} + e_l P_l S_L d\sigma_{LL}^I + P_l S_L d\sigma_{LL}^{DVCS} \\ & + P_l S_T d\sigma_{LT}^{BH} + e_l P_l S_T d\sigma_{LT}^I + P_l S_T d\sigma_{LT}^{DVCS} \end{aligned}$$


Bethe-Heitler contribution:

 calculated at QED

DVCS contribution:

 HERMES: $|\mathcal{T}_{DVCS}|^2 \ll |\mathcal{T}_{BH}|^2$

interference term:

 depend on a linear combination of Compton form factors

 access to GPD combinations through azimuthal asymmetries

express asymmetries in terms of Fourier coefficients

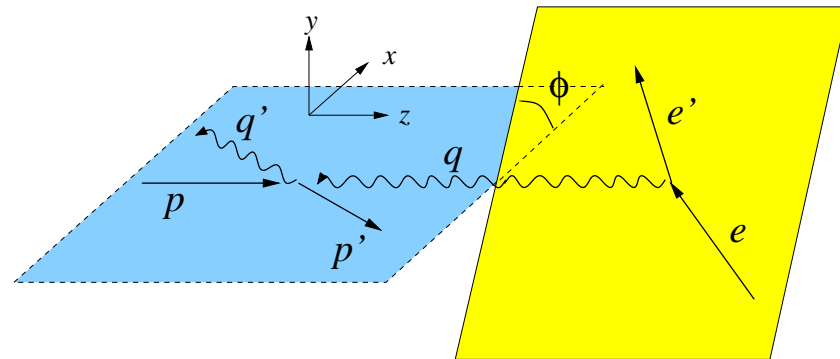
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

Fourier expansion in azimuthal angle ϕ

$$|\tau_{BH}|^2 \propto \sum_{n=0}^2 c_n^{BH} \cos(n\phi)$$

$$|\tau_{DVCS}|^2 \propto \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + P_\ell s_1^{DVCS} \sin \phi$$

$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



express asymmetries in terms of Fourier coefficients

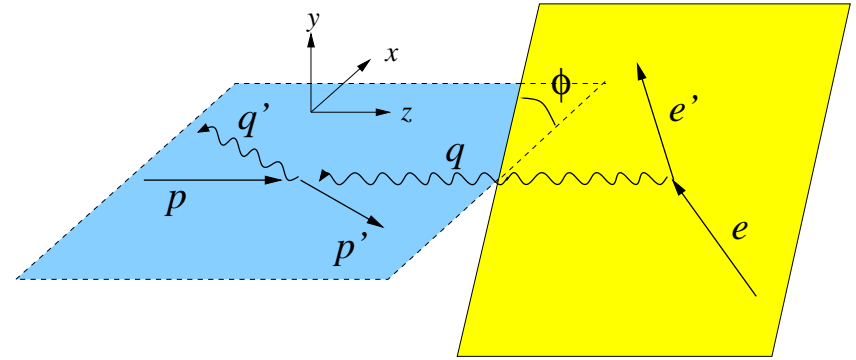
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

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$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



$$c_1^I \propto F_1 \text{Re}\mathcal{H}$$

$$c_0^I \propto -\frac{-t}{Q} c_1^I$$

$$s_1^I \propto F_1 \text{Im}\mathcal{H}$$

express asymmetries in terms of Fourier coefficients

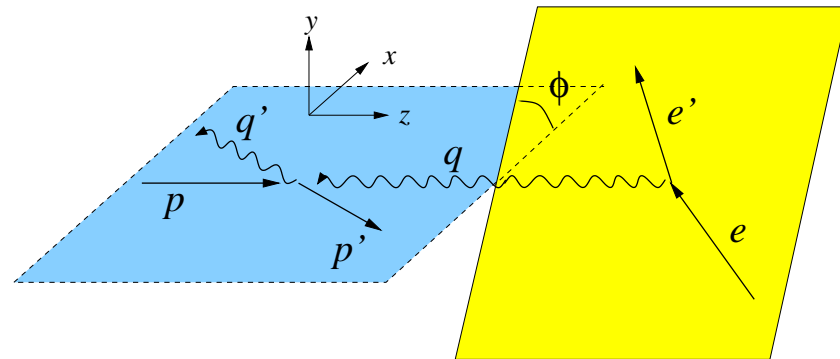
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

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$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



DVCS term:

azimuthal modulation	$\gamma^*(\mu) \rightarrow \gamma(\mu')$	relative order
constant	$+1 \rightarrow +1$	1
$\cos \phi, \sin \phi$	$0 \rightarrow +1$	$1/Q$
$\cos 2\phi, \sin 2\phi$	$-1 \rightarrow +1$	1 (gluon GPDs) $1/Q^2$ (quark GPDs)

$$c_1^I \propto F_1 \text{Re}\mathcal{H}$$

$$c_0^I \propto -\frac{-t}{Q} c_1^I$$

$$s_1^I \propto F_1 \text{Im}\mathcal{H}$$

express asymmetries in terms of Fourier coefficients

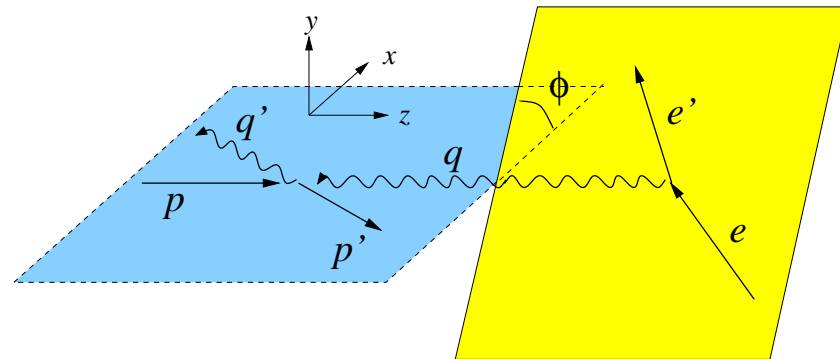
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

Fourier expansion in azimuthal angle ϕ

$$|\tau_{BH}|^2 \propto \sum_{n=0}^2 c_n^{BH} \cos(n\phi)$$

$$|\tau_{DVCS}|^2 \propto \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + P_\ell s_1^{DVCS} \sin \phi$$

$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



interference term:

azimuthal modulation	$\gamma^*(\mu) \rightarrow \gamma(\mu')$	relative order
constant	$+1 \rightarrow +1$	$1/Q$
$\cos \phi, \sin \phi$	$+1 \rightarrow +1$	1
$\cos 2\phi, \sin 2\phi$	$0 \rightarrow +1$	$1/Q$
$\cos 3\phi, \sin 3\phi$	$-1 \rightarrow +1$	$1/Q^2$ or α_s

$$c_1^I \propto F_1 \text{Re}\mathcal{H}$$

$$c_0^I \propto -\frac{t}{Q} c_1^I$$

$$s_1^I \propto F_1 \text{Im}\mathcal{H}$$

DVCS at HERMES (pre-recoil data)

$$e + p \rightarrow e' + \gamma + p'$$

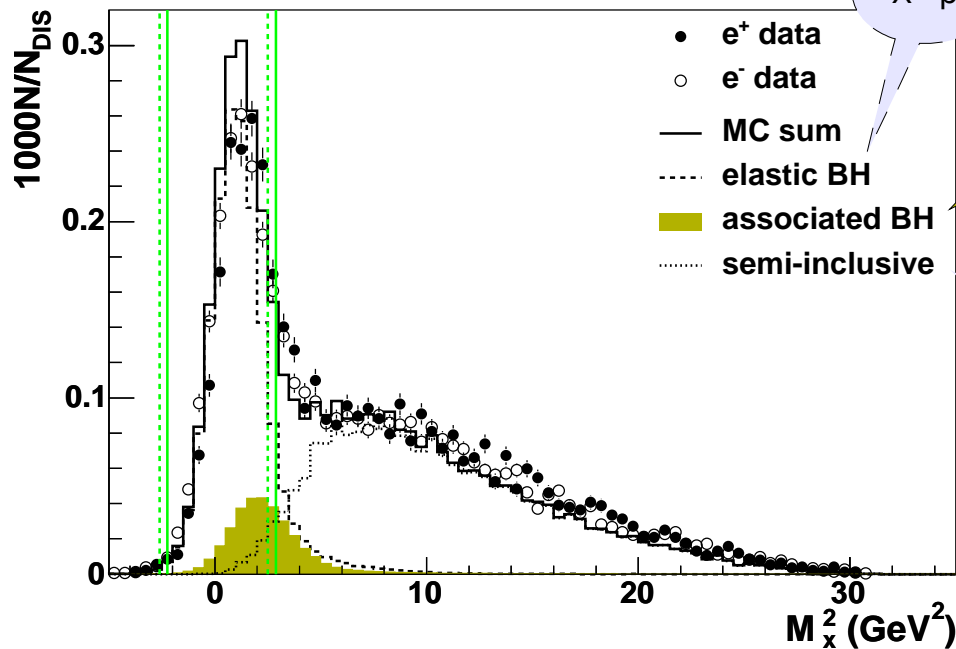
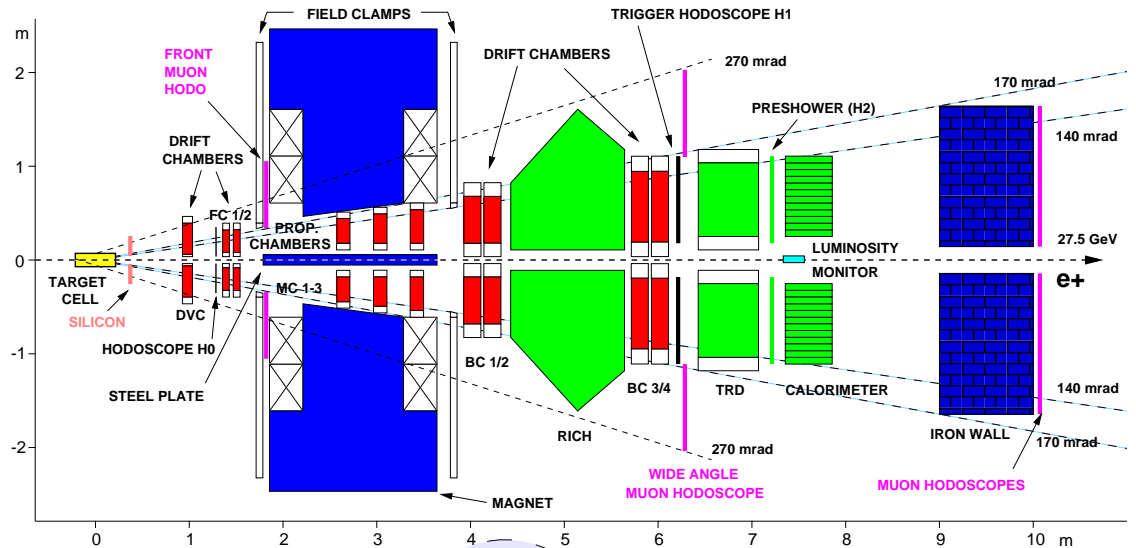


detected particles:
lepton and photon



missing mass technique for
 $ep \rightarrow e'\gamma X$:

$$M_X^2 = (p + e - e' - \gamma)^2$$



$X=p$

Resonant excitation:
 $X=\Delta^+$

$X=\pi^0 + \dots$

unpolarized-target asymmetries

$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell \mathcal{A}_{LU}^{DVCS}(\phi) + e_\ell P_\ell \mathcal{A}_{LU}^I(\phi) + e_\ell \mathcal{A}_C(\phi) \right]$$

beam-helicity asymmetry (single charge):

$$\mathcal{A}_{LU}(\phi) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

- projects the imaginary part of τ_{DVCS}
- no separate access to s_1^{DVCS} and s_1^I

beam-helicity asymmetry (new approach):

- charge-difference beam-helicity asymmetry

$$\mathcal{A}_{LU}^I(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

- charge-averaged beam-helicity asymmetry

$$\mathcal{A}_{LU}^{DVCS}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

- s_1^{DVCS} and s_1^I can be disentangled

beam-charge asymmetry:

$$\mathcal{A}_C(\phi) \equiv \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-}$$

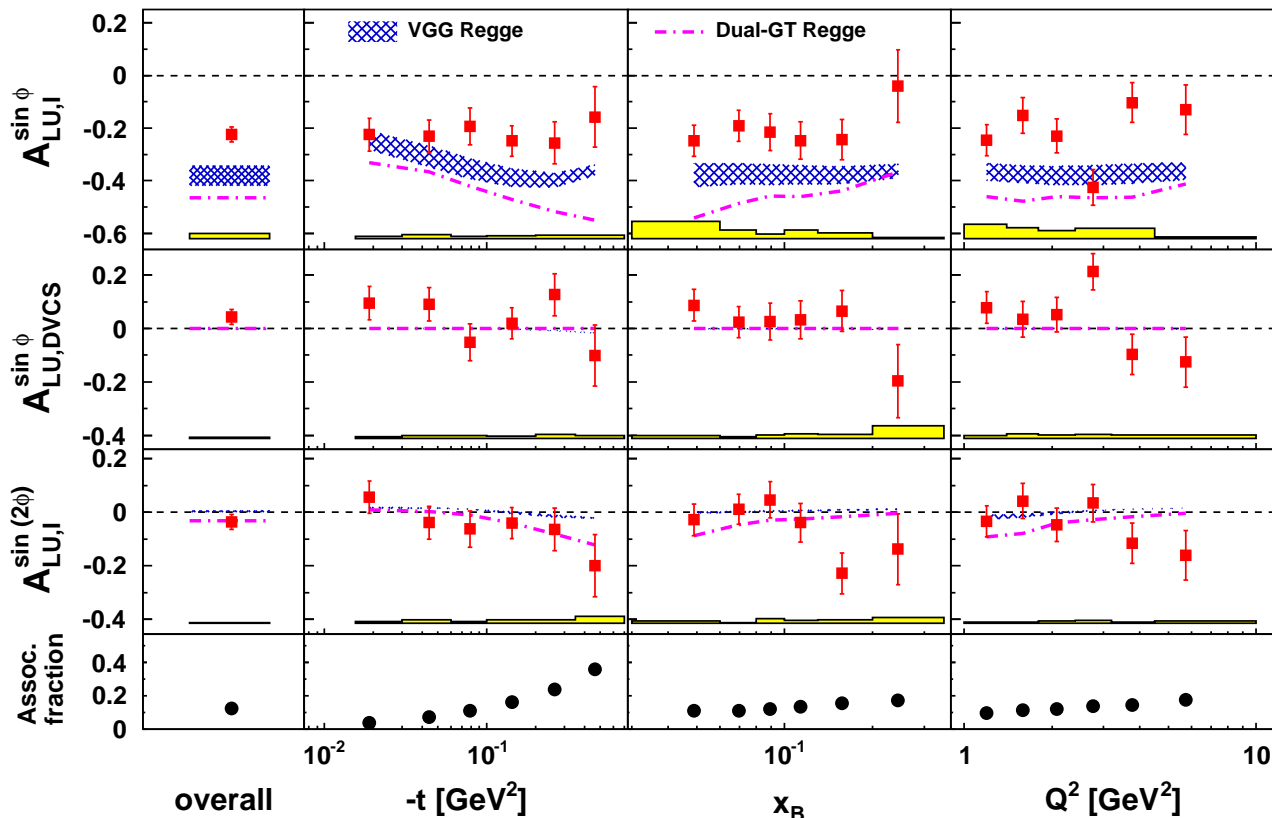
- projects the real part of τ_{DVCS}

beam helicity asymmetry

$$A_{LU}^I(\phi) = \sum_{n=1}^2 A_{LU,I}^{\sin(n\phi)} \sin(n\phi) \propto \sum_{n=1}^2 s_n^I \sin(n\phi)$$

$$A_{LU,DVCS}^{\sin\phi} \propto s_1^{DVCS} \sin\phi$$

-HERMES Collaboration: arXiv:0909.3587 (2009)-



$$A_{LU,I}^{\sin\phi}$$



twist-2:

$$\propto F_1 \text{Im}\mathcal{H}$$



large overall value



no kin. dependencies

$$A_{LU,DVCS}^{\sin\phi}, A_{LU,I}^{\sin 2\phi}$$



twist-3



overall value

compatible with 0



no kin. dependencies



overshoot the magnitude of $A_{LU,I}^{\sin\phi}$ by a factor of 2



describe the shape of kin dependencies on x_B and Q^2 , but not on t

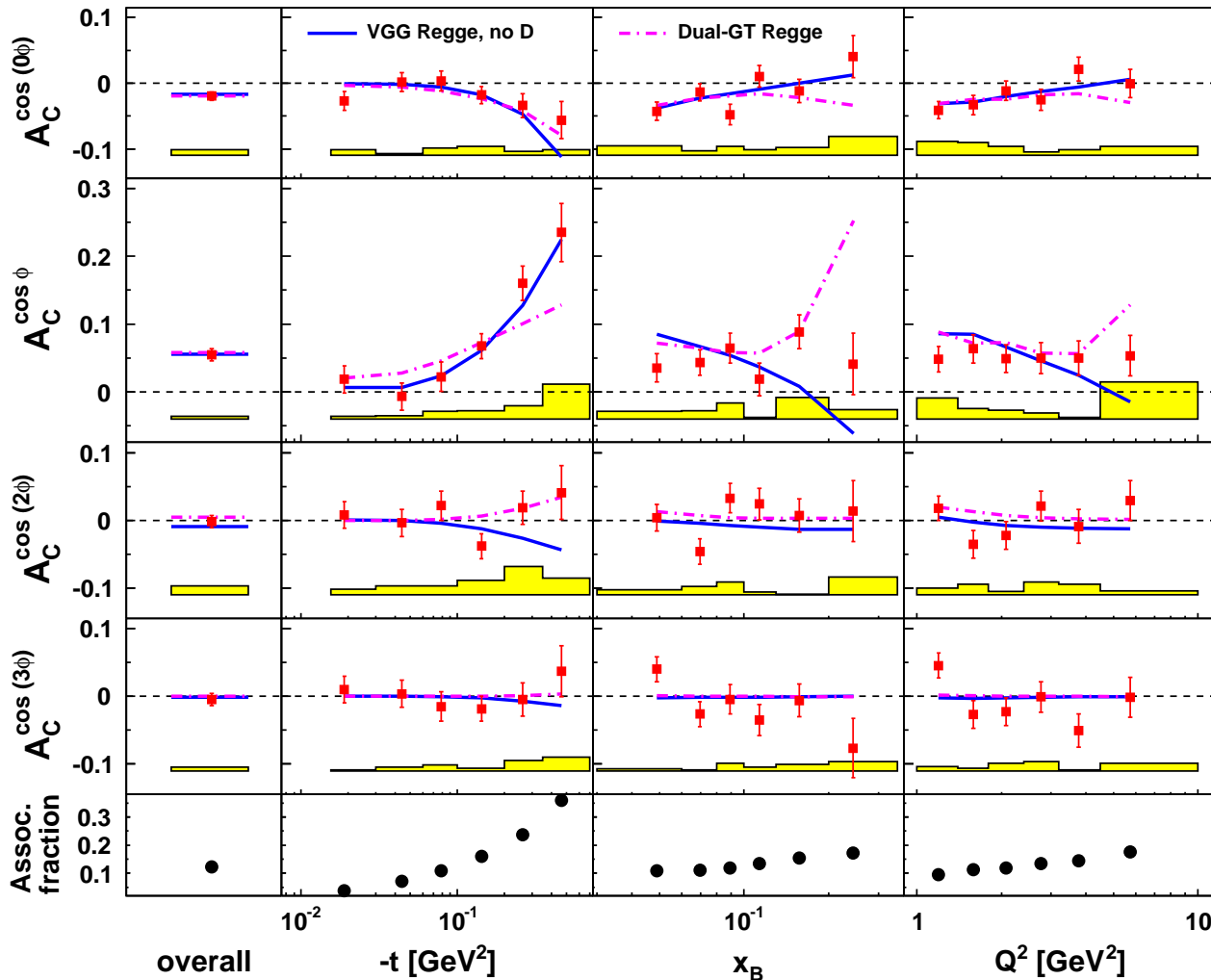


overestimation is not due to the associated production

beam charge asymmetry

$$A_C(\phi) = \sum_{n=0}^3 A_C^{\cos(n\phi)} \cos(n\phi) \propto \sum_{n=0}^3 c_n^I \cos(n\phi)$$

-HERMES Collaboration: arXiv:0909.3587 (2009)-



twist-2 $A_C^{\cos \phi}$, twist-3 $A_C^{\cos 0\phi}$

- strong t -dependence
- no x_B , Q^2 dependencies

$$A_C^{\cos \phi} \propto F_1 \text{Re}\mathcal{H}$$

$$A_C^{\cos 0\phi} \propto -\frac{t}{Q} A_C^{\cos \phi}$$

$A_C^{\cos(2\phi)} \approx 0$: twist-3 GPDs

$A_C^{\cos(3\phi)} \approx 0$: gluon helicity-flip GPDs

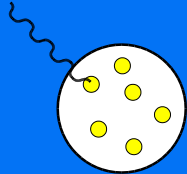
theoretical predictions:

- does not describe the beam-helicity data, but in good agreement with this data

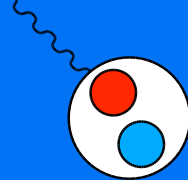
unpolarized deuterium targets

coherent: $e^\pm d \rightarrow e^\pm d \gamma$

 DVCS



 Bethe-Heitler



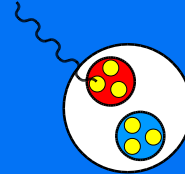
 target stays intact

 spin-1 targets described by 9 GPDs:

$$H_1^q, H_2^q, H_3^q, H_4^q, H_5^q, \tilde{H}_1^q, \tilde{H}_2^q, \tilde{H}_3^q, \tilde{H}_4^q$$

incoherent: $e^\pm d \rightarrow e^\pm pn \gamma$

 DVCS

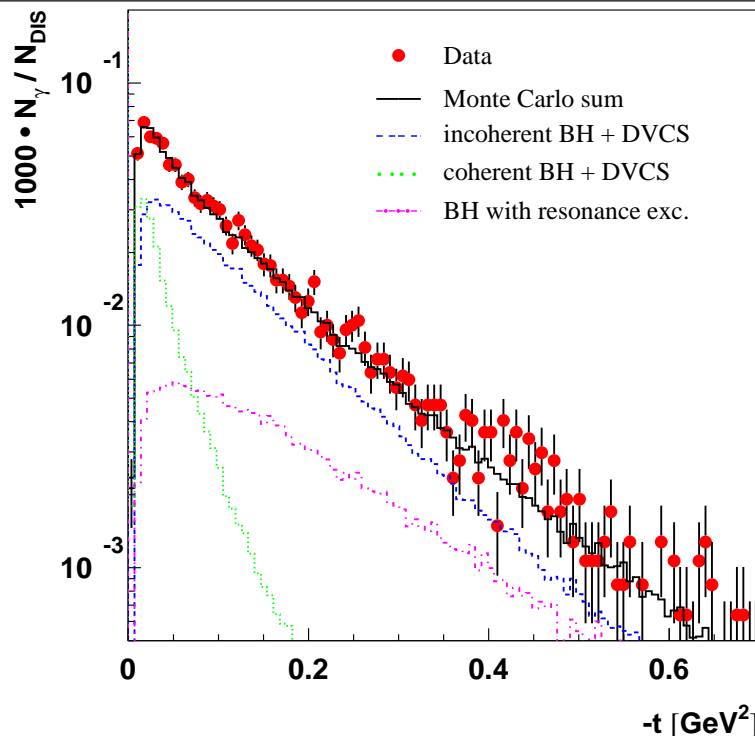
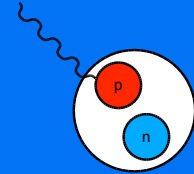


 target brakes up

 spin- $\frac{1}{2}$ targets described by 4 GPDs:

$$H, E, \tilde{H}, \tilde{E}$$

 Bethe-Heitler




coherent:

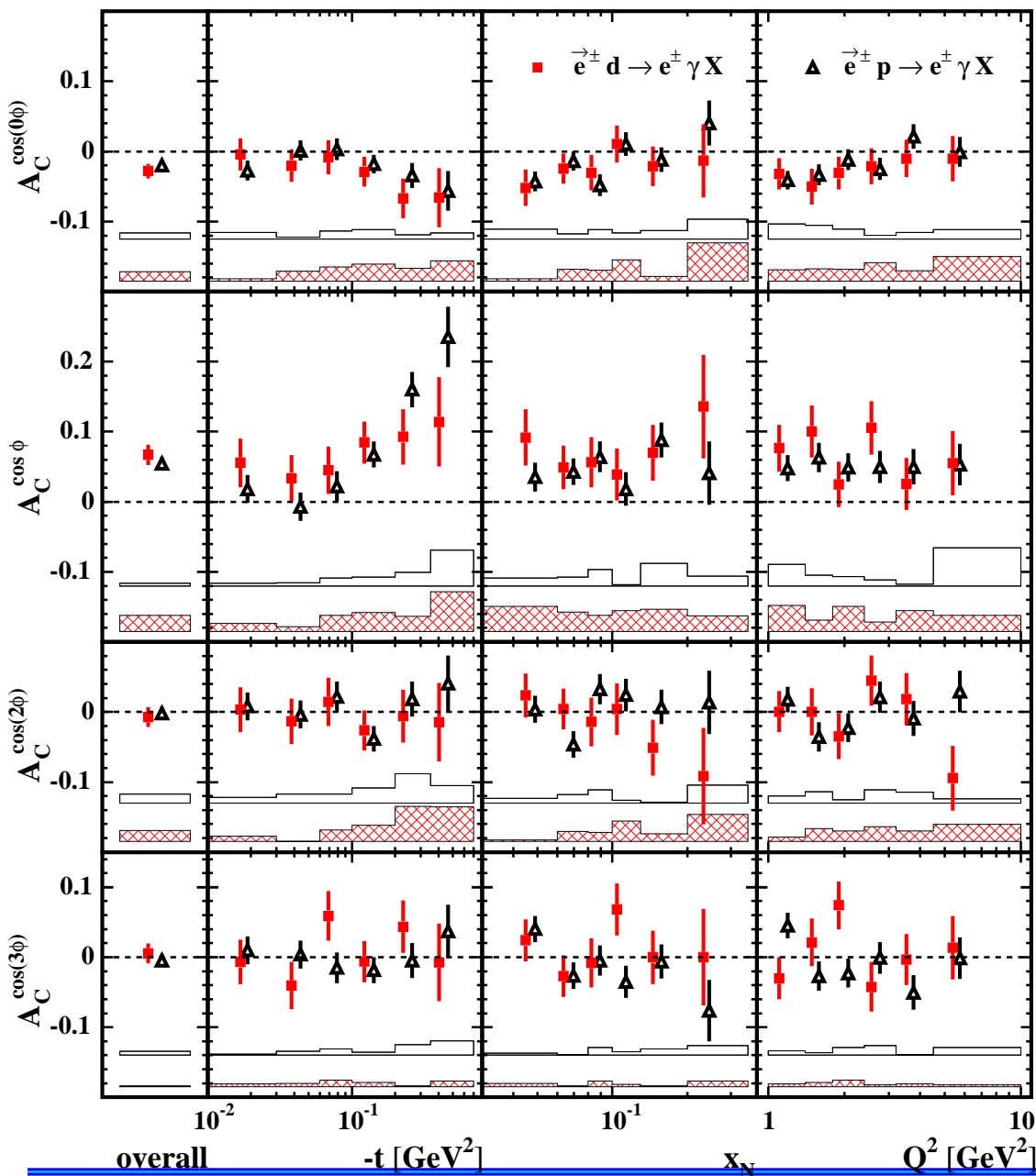
 contribution at small $-t$

incoherent:

 contribution at larger $-t$

 contribution from coherent $[0.06 : 0.7] \text{ GeV}^2$:
20%

beam-charge asymmetry



$$A_C(\phi) = \sum_{n=0}^3 A_C^{\cos(n\phi)} \cos(n\phi)$$

-HERMES Collaboration: arXiv:0911.0091 (2009)-

twist-2:

$$A_{C,coh}^{\cos \phi} \propto G_1 \text{Re}\mathcal{H}_1$$




$$A_{C,incoh}^{\cos \phi} \propto F_1 \text{Re}\mathcal{H}$$

higher twist :

$$A_C^{\cos 0\phi} \propto -\frac{t}{Q} A_C^{\cos \phi}$$

$$A_C^{\cos(2\phi)} \approx 0$$

$$A_C^{\cos(3\phi)} \approx 0$$

-  d and p results consistent
-  small values of $-t$: differences due to coherent contribution
-  larger values of $-t$: differences due to neutron contribution

longitudinal target polarization

$$\sigma(\phi, P_\ell, S_L) = \sigma_{UU}(\phi) \times [1 + P_\ell \mathcal{A}_{LU} + S_L \mathcal{A}_{UL}(\phi) + S_L P_\ell \mathcal{A}_{LL}(\phi)]$$

beam helicity asymmetry:

$$\mathcal{A}_{LU}(\phi) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

 projects the imaginary part of τ_{DVCS}

 no separate access to s_1^{DVCS} and s_1^I

longitudinal target-spin asymmetry:

$$\mathcal{A}_{UL}(\phi) \equiv \frac{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Rightarrow}) - (d\sigma^{\rightarrow\Leftarrow} + d\sigma^{\leftarrow\Leftarrow})}{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Rightarrow}) + (d\sigma^{\rightarrow\Leftarrow} + d\sigma^{\leftarrow\Leftarrow})}$$

 projects the imaginary part of τ_{DVCS}

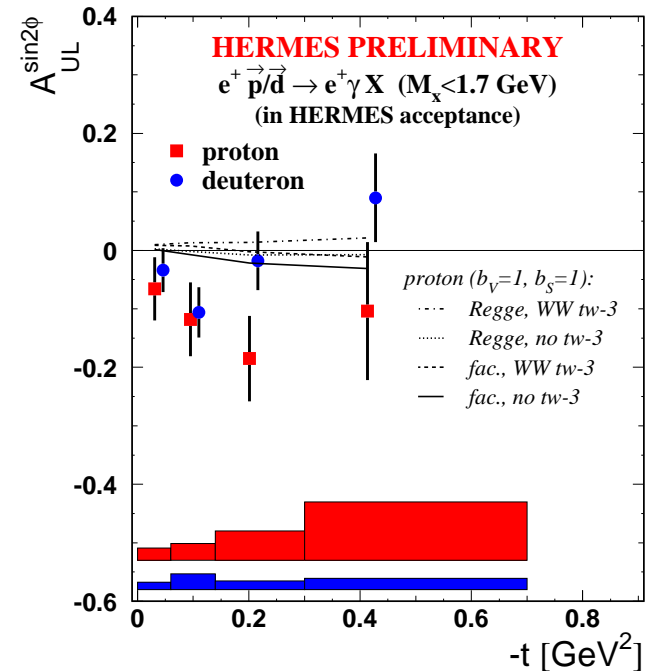
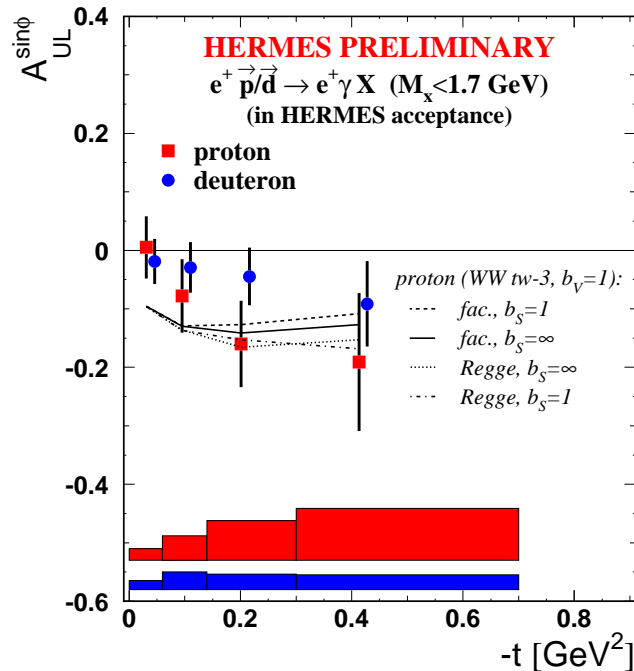
double-spin asymmetry:

$$\mathcal{A}_{LL}(\phi) \equiv \frac{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Leftarrow}) - (d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Leftarrow})}{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Leftarrow}) + (d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Leftarrow})}$$

 projects the real part of τ_{DVCS}

longitudinal target-spin asymmetry

$$A_{UL}(\phi) = \sum_{n=1}^2 A_{UL}^{\sin(n\phi)} \sin(n\phi) \propto \sum_{n=1}^2 s_n^I, s_n^{\text{DVCS}}$$



● s_1^I : twist-2

$$A_{UL}^{\sin \phi} \propto s_1^I \propto F_1 \text{Im} \tilde{\mathcal{H}}$$

● s_1^{DVCS} : twist-3

model in good agreement with data

unexpected large value

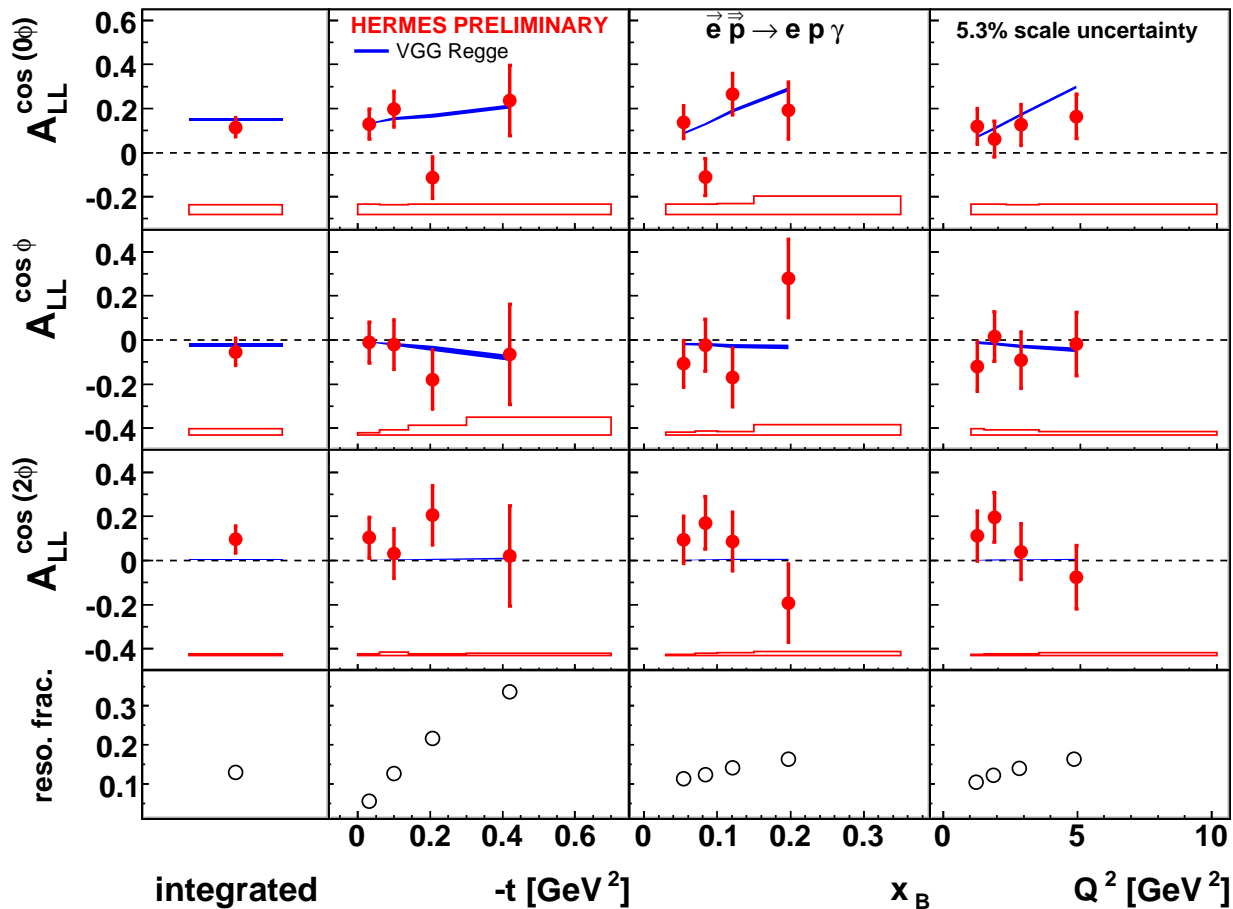
● s_2^I : quark twist-3 or gluon twist-2

● s_2^{DVCS} : twist-4

model does not describe the data

double-spin asymmetry

$$A_{LL}(\phi) \propto \sum_0^2 A_{LL}^{\cos(n\phi)} \cos(n\phi) \propto \sum_{n=0}^2 c_n^I, c_n^{\text{DVCS}}$$



twist-2: $\propto F_1 \text{Re}\tilde{\mathcal{H}}$

$$A_{LL}^{\cos 0\phi} \propto \begin{cases} c_0^{\text{DVCS}} \\ c_0^I \end{cases}$$



twist-2 / twist-3:

$$A_{LL}^{\cos \phi} \propto \begin{cases} c_1^{\text{DVCS}} \\ c_1^I \end{cases}$$

twist-3:

$$A_{LL}^{\cos 2\phi} \propto c_2^I$$

model predictions:

-  the same model, as for BCA and BHA
-  in good agreement with data

transversely polarized target

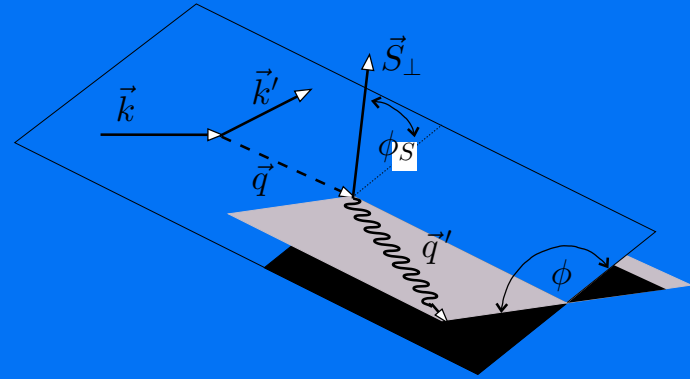
$$\sigma(\phi, P_\ell, S_T) = \sigma_{UU}(\phi) \times \left[1 + S_T \mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) + S_T e_\ell \mathcal{A}_{UT}^{\text{I}}(\phi, \phi_S) + e_\ell \mathcal{A}_C(\phi) \right]$$

transverse target-spin asymmetry:

$$\mathcal{A}_{UT}(\phi, \phi_S) = \frac{1}{S_T} \cdot \frac{d\sigma^{\uparrow}(\phi, \phi_S) - d\sigma^{\downarrow}(\phi, \phi_S)}{d\sigma^{\uparrow}(\phi, \phi_S) + d\sigma^{\downarrow}(\phi, \phi_S)}$$

beam-charge asymmetry:

$$\mathcal{A}_C(\phi) \equiv \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-}$$



$$\mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) \equiv \frac{1}{S_T} \cdot \frac{d\sigma^{+\uparrow}(\phi, \phi_S) - d\sigma^{+\downarrow}(\phi, \phi_S) + d\sigma^{-\uparrow}(\phi, \phi_S) - d\sigma^{-\downarrow}(\phi, \phi_S)}{d\sigma^{+\uparrow}(\phi, \phi_S) + d\sigma^{+\downarrow}(\phi, \phi_S) + d\sigma^{-\uparrow}(\phi, \phi_S) + d\sigma^{-\downarrow}(\phi, \phi_S)}$$

$$\mathcal{A}_{UT}^{\text{I}}(\phi, \phi_S) \equiv \frac{1}{S_T} \cdot \frac{d\sigma^{+\uparrow}(\phi, \phi_S) - d\sigma^{+\downarrow}(\phi, \phi_S) - d\sigma^{-\uparrow}(\phi, \phi_S) + d\sigma^{-\downarrow}(\phi, \phi_S)}{d\sigma^{+\uparrow}(\phi, \phi_S) + d\sigma^{+\downarrow}(\phi, \phi_S) + d\sigma^{-\uparrow}(\phi, \phi_S) + d\sigma^{-\downarrow}(\phi, \phi_S)}$$

separation of $s_i^{\text{DVCS}}, c_i^{\text{DVCS}}$ and $s_i^{\text{I}}, c_i^{\text{I}}$ terms with same harmonic signatures

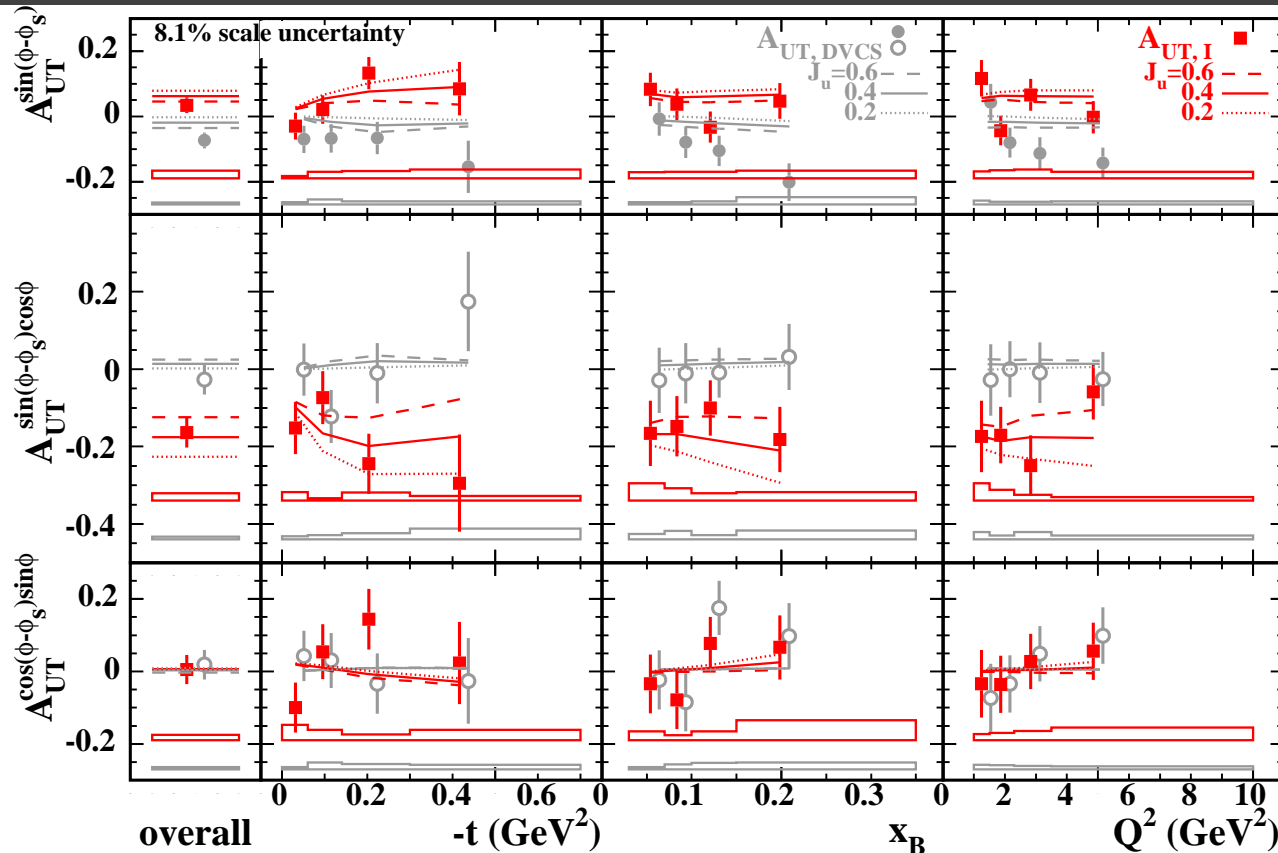
projects the imaginary part of τ_{DVCS}

transverse target-spin asymmetry

$$\begin{aligned}\mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) &= \sum_{n=0}^2 A_{UT, \text{DVCS}}^{\sin(\phi - \phi_S) \cos(n\phi)} \sin(\phi - \phi_S) \cos(n\phi) \\ &+ \sum_{n=1}^2 A_{UT, \text{DVCS}}^{\cos(\phi - \phi_S) \sin(n\phi)} \cos(\phi - \phi_S) \sin(n\phi) \\ \mathcal{A}_{UT}^{\text{I}}(\phi, \phi_S) &= \sum_{n=0}^2 A_{UT, \text{I}}^{\sin(\phi - \phi_S) \cos(n\phi)} \sin(\phi - \phi_S) \cos(n\phi) \\ &+ \sum_{n=1}^2 A_{UT, \text{I}}^{\cos(\phi - \phi_S) \sin(n\phi)} \cos(\phi - \phi_S) \sin(n\phi)\end{aligned}$$

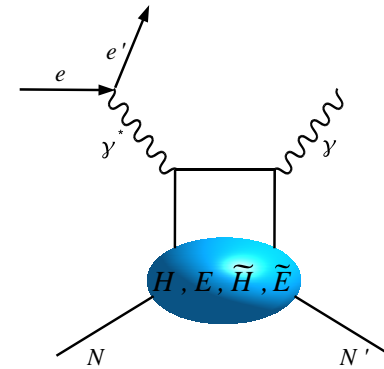
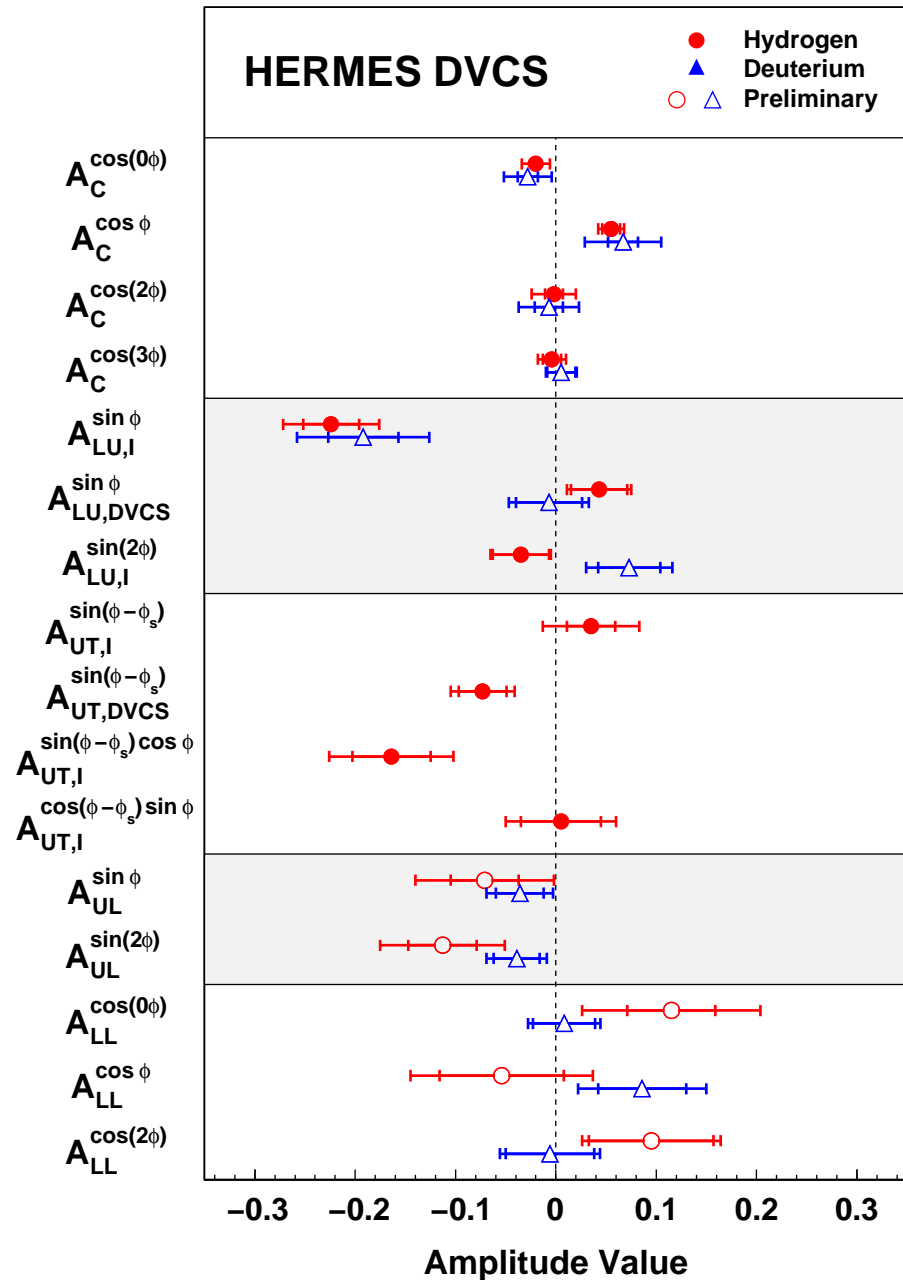
transverse target-spin asymmetry

$$A_{UT}(\phi, \phi_S) \propto \text{Im}[F_2\mathcal{H} - F_1\mathcal{E}] \sin(\phi - \phi_S) \cos \phi + \text{Im}[F_2\mathcal{H} - F_1\mathcal{E}] \sin(\phi - \phi_S) \\ + \text{Im}[\mathcal{H}\mathcal{E}^* - \mathcal{E}\mathcal{H}^* + \xi\tilde{\mathcal{E}}\tilde{\mathcal{H}}^* - \tilde{\mathcal{H}}\xi\tilde{\mathcal{E}}^*] \sin(\phi - \phi_S) + \dots$$



- $A_{UT}^{\sin(\phi - \phi_S) \cos \phi}$ found much more sensitive to J_u than others
- insensitive to J_d , assumed $J_d = 0$ (supported by lattice QCD)
- with a good model, allows a model-dependent constraint

Summary



beam-charge asymmetry:

$\text{Re}\mathcal{H}$

beam-helicity asymmetry:

$\text{Im}\mathcal{H}$

transverse target-spin asymmetry:

$\text{Im}(\mathcal{H}\mathcal{E})$

longitudinal target-spin asymmetry:

$\text{Im}\tilde{\mathcal{H}}$

double-spin asymmetry:

$\text{Re}\tilde{\mathcal{H}}$

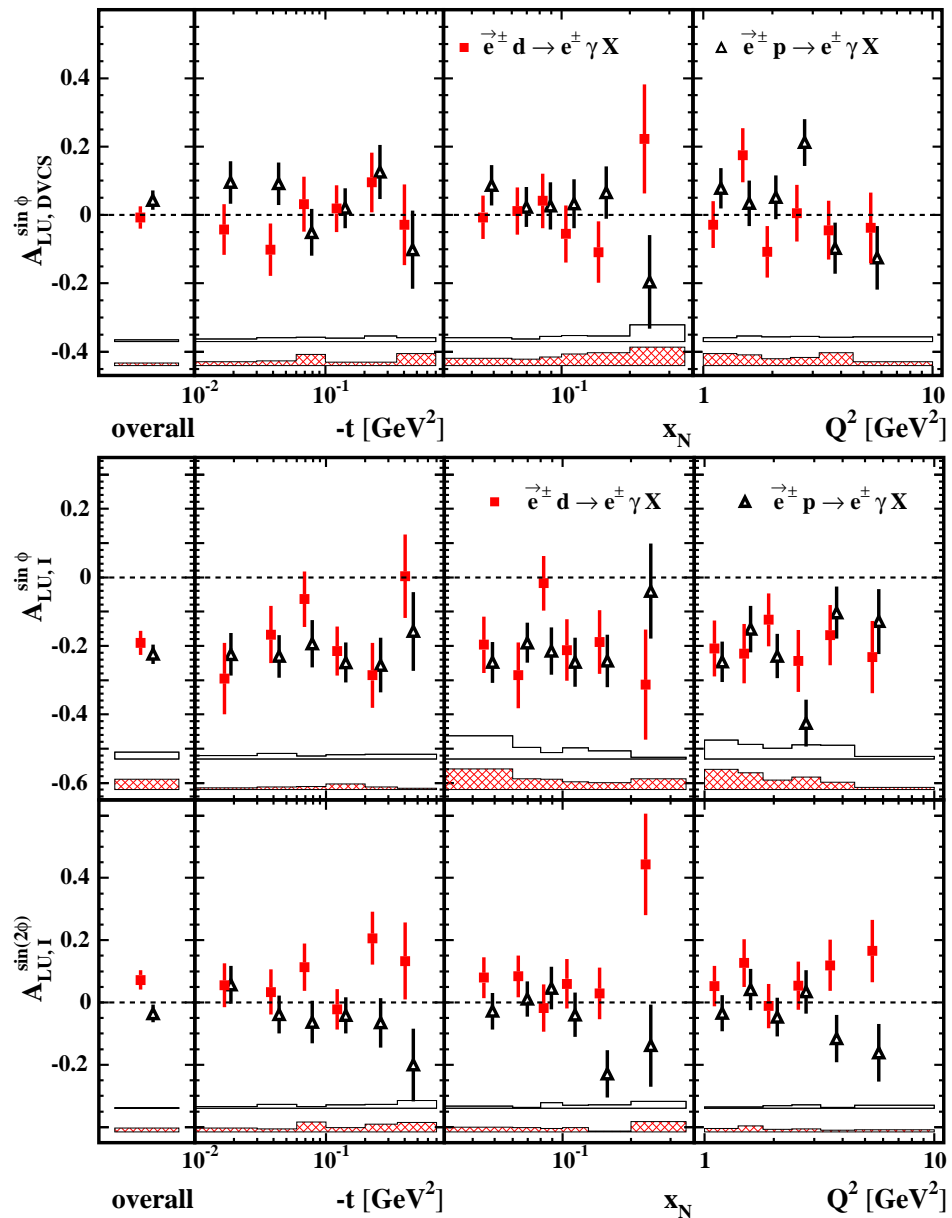
backup slides

beam helicity asymmetry

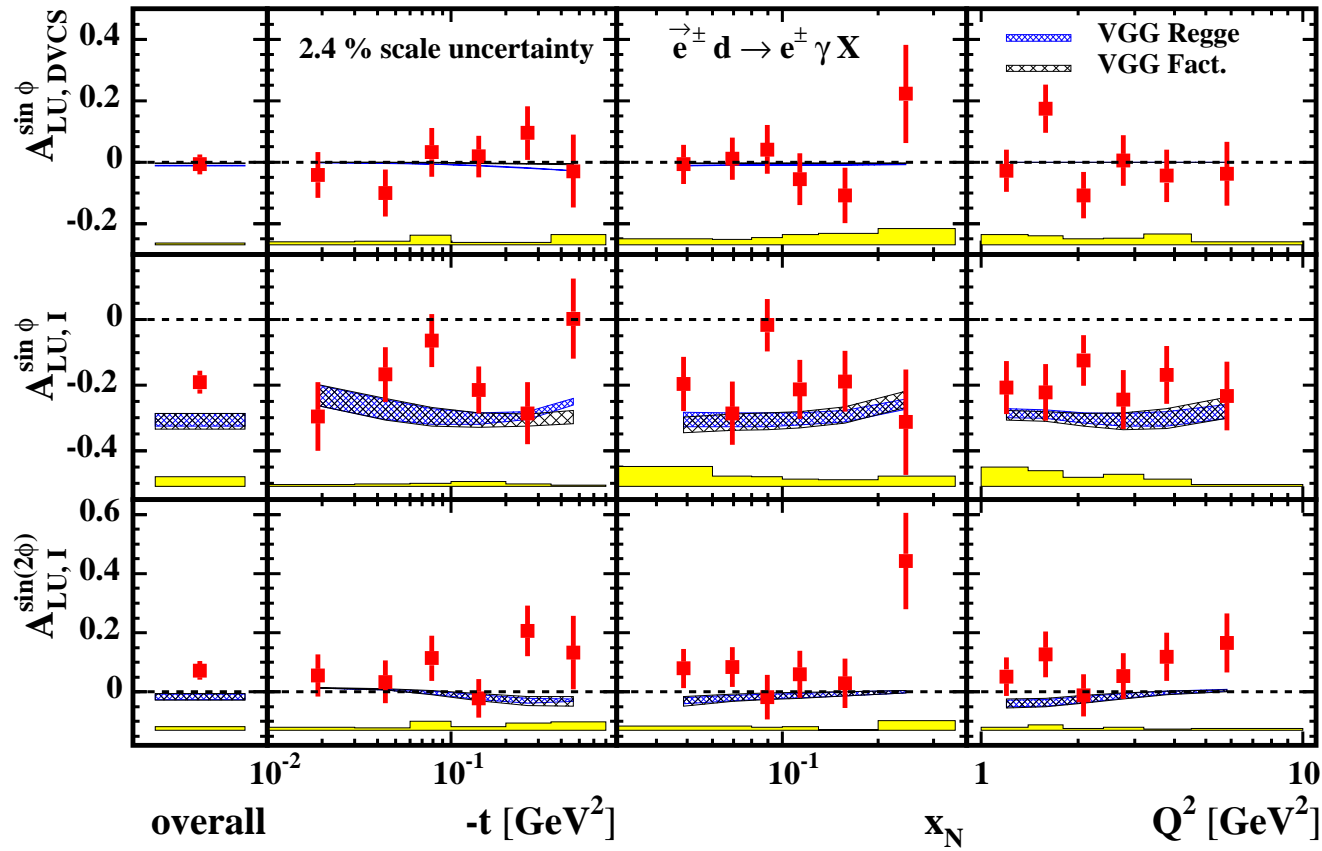
$$\begin{aligned}
 A_{LU}(\phi) &\equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}} \\
 &= \frac{-e_{\ell} \frac{K_I}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=1}^2 s_n^I \sin(n\phi) \right] + \frac{1}{Q^2} s_1^{\text{DVCS}} \sin \phi}{\frac{1}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[K_{\text{BH}} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi) - e_{\ell} K_I \sum_{n=0}^3 c_n^I \cos(n\phi) \right] + \frac{1}{Q^2} \sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi)}.
 \end{aligned}
 \tag{1}$$

$$\begin{aligned}
 A_{LU}^I(\phi) &\equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})} \\
 &= \frac{-\frac{K_I}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=1}^2 s_n^I \sin(n\phi) \right]}{\frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi) + \frac{1}{Q^2} \sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi)},
 \end{aligned}
 \tag{2}$$

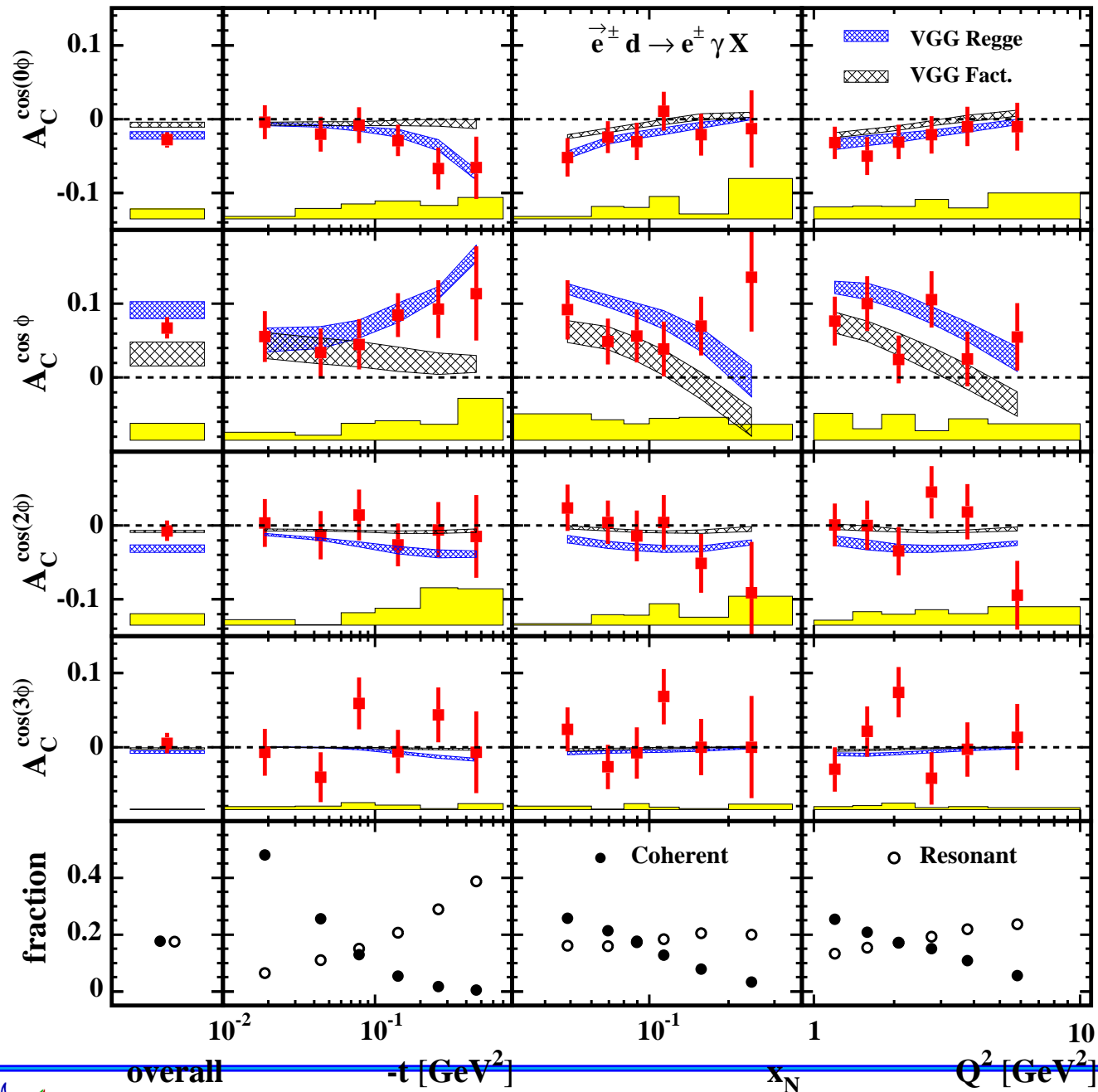
beam-helicity asymmetry



beam-helicity asymmetry



beam-helicity asymmetry



nuclear targets: He, N, Ne, Kr, Xe

